

1. Vypočítajte integrál $\int_K \frac{e^z}{z^2+3z+2} dz$
 - a) K je JUPCHK \oplus , $-1 \in \text{int } K$, $-2 \in \text{ext } K$.
 - b) K je JUPCHK \ominus , $-1, -2 \in \text{int } K$
 - c) K je JUPCHK \oplus , $-1, -2 \in \text{ext } K$
2. Vypočítajte integrál $\int_K \frac{z}{(z+2)(z+1)^2} dz$
 - a) K je JUPCHK \ominus , $-1 \in \text{int } K$, $-2 \in \text{ext } K$.
 - b) K je JUPCHK \oplus , $-1, -2 \in \text{int } K$
 - c) K je JUPCHK \oplus , $-1, -2 \in \text{ext } K$
3. Nájdite lineárne lomené zobrazenie $f(z)$, pre ktoré:
 - a. $f(i) = -1, f(1+i) = i, f(1) = \infty$. [$\left[\left[\frac{(i-2)z+2+i}{z-1} \right] \right]$
 - b. $f(-1) = i, f(i) = 1+i, f(\infty) = 1$. [$\left[\left[\frac{z+2+i}{z+2-i} \right] \right]$
 - c. $f(-i) = 0, f(0) = \frac{1}{2}(1-i), f(-i) = 0$. [$\left[\left[\frac{iz-1}{2z+i+1} \right] \right]$
 - d. $f(-1) = -\frac{1}{2}i, f(i) = \frac{1}{2}(-1+i), f(2) = i$. [$\left[\left[\frac{i}{z-1} \right] \right]$
 - e. $f(i) = -\frac{1}{3}, f(-2i) = \infty, f(\infty) = 2$. [$\left[\left[\frac{2z-i}{z+2i} \right] \right]$
4. Nájdite lineárne lomené zobrazenie $f(z)$, ktoré zobrazí
 - a. $\{z \in C: \text{Re } z > 1\} \rightarrow \{z \in C: |z-2| > 1\}$ [$\left[\left[\frac{z-4}{z-2} \right] \right]$
 - b. $\{z \in C: \text{Re } z > 0\} \rightarrow \{z \in C: \text{Re } z < 0\}$ [$\left[\left[f(z) = -z \right] \right]$
 - c. $\{z \in C: \text{Re } z > 0\} \rightarrow \{z \in C: |z| < 1\}$ [$\left[\left[\frac{z-1}{z+1} \right] \right]$
 - d. $\{z \in C: \text{Re } z > 0\} \rightarrow \{z \in C: |z| > 1\}$ [$\left[\left[\frac{z+1}{z-1} \right] \right]$
 - f. $\{z \in C: |z| < 1\} \rightarrow \{z \in C: \text{Im } z < 0\}$ [$\left[\left[\frac{iz+1}{z+i} \right] \right]$
 - e. $\{z \in C: |z| > 1\} \rightarrow \{z \in C: \text{Im } z < 0\}$ [$\left[\left[\frac{z+i}{iz+1} \right] \right]$
5. Ukážte, že funkcia f je analytická v oblasti M a určte $\max_M f(z)$, ak
 - a. $M = \{z \in C: \text{Re } z \leq 0\}, f(z) = \frac{e^z}{z-1}$ [$\left[\left[1 \right] \right]$
 - b. $M = \{z \in C: 0 \leq \text{Re } z \leq 1\}, f(z) = \frac{2}{z-2}$ [$\left[\left[2 \right] \right]$
 - c. $M = \{z \in C: \text{Re } z \geq 1\}, f(z) = \frac{2}{z^2+1}$ [$\left[\left[1 \right] \right]$
 - d. $M = \{z \in C: 1 \leq \text{Re } z \leq 5\}, f(z) = \frac{1}{z^2+z}$ [$\left[\left[1/2 \right] \right]$
6. Určte $\max_M f(z)$ $\min_M f(z)$, ak
 - a. $M = \{z \in C: |z| \leq 2\}, f(z) = z^2 + 5$ [$\left[\left[1, 9 \right] \right]$
 - b. $M = \{z \in C: |z| \leq 4\}, f(z) = z^2 + 10$ [$\left[\left[0, 26 \right] \right]$
 - c. M je trojuholník s vrcholmi $z = 0, z = \frac{\pi}{2}, z = i\frac{\pi}{2}; f(z) = e^z + 4$ [$\left[\left[\min = \sqrt{17}, \max = e^{(\pi/2)} + 4 \right] \right]$
 - d. M je obdĺžnik $-1 \leq x \leq 1, 0 \leq y \leq 1, f(z) = z^2 + 4$ [$\left[\left[3, 5 \right] \right]$
7. Určte $\max_D f(z), \min_D f(z), f(D)$ a $f(M)$, ak $D = \{z \in C: |z| \leq 1\}, M = \{z \in C: \text{Re } z \geq 0\}$.
 - a. $f(z) = \frac{2z-i}{2+iz}$
 - b. $f(z) = \frac{(2z-i)^2}{(2+iz)^2}$
 - c. $f(z) = \frac{z+2i}{2iz-4}$
8. Vypočítajte komplexný Fourierov rad funkcie f .
 - a. $f(t) = t, t \in \langle 0, 1 \rangle$
 - b. $f(t) = t, t \in \langle -1, 1 \rangle$
 - c. $f(t) = |t|, t \in \langle -1, 1 \rangle$
 - d. $f(t) = e^t, t \in \langle -1, 1 \rangle$
 - e. $f(t) = \begin{cases} 1+t, & t \in \langle -1, 0 \rangle, \\ 1-t, & t \in \langle 0, 1 \rangle \end{cases}$
 - f. $f(t) = t^2, t \in \langle -1, 1 \rangle$